

X-RAY OPTICAL COMPONENTS FOR HARD X-RAY SYNCHROTRON RADIATION SOURCES



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National School for Neutron and X-ray Scattering August 2017

OUTLINE

Outline of Presentation

- 1. Why Do We Need Optics?
- 2. X-ray Mirrors (Reflective Optics)
- 3. Perfect Crystal X-ray Optics (Diffractive Optics)
- 4. Focusing Optics (Reflective, Diffractive and Refractive)

I will not be talking about gratings as they are used in the soft x-ray region of the spectrum and the focus of this talk will be hard x-ray optics.



WHY DO WE NEED OPTICS?

- Control the energy (E) and bandwidth (∆E) of the beam.
 - $\Delta E = 1-2 \text{ eV} @ 10 \text{ keV}; \Delta E/E = 10^{-4}$ (typical diffraction exp.)
 - ΔE = 1-2 keV @ 10 keV; ΔE/E = 10⁻¹ (timeresolved studies)
 - ΔE = a few milli-eV @ 10 keV; ΔE/E = 10⁻⁷ (inelastic scattering earlier today)
- Control the size/divergence of the beam (often related).
 - Micro or nano beams (spot sizes microns to 10's of nanometers)
 - Highly collimated beams
- Control the polarization of the beam.
 - Linear
 - Circular (see talk on x-ray magnetic dichroism)







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INDEX OF REFRACTION FOR X-RAYS: N < 1

This expression for the (real part) index of refraction:

n =
$$[1 - (n_e(e^2/mc^2)\lambda^2/\pi)]^{1/2} \approx 1 - (n_e r_e/2\pi)\lambda^2$$

is usually written as:

n = 1 -
$$\delta$$
, where $\delta = (n_e r_e/2\pi)\lambda^2$.

and $r_e = (e^2/mc^2)$ is the classical radius of the electron (2.82 x 10⁻¹³ cm), n_e is the electron density, and λ is the wavelength of the x-ray.

When you plug in the numbers for the real part of the index of refraction you find:

$$\delta = 10^{-5}$$
 to 10^{-6}

So you have:

an index of refraction less than one differing from unity by only a few ppm

This simple treatment does not include any absorption. A more detailed calculation would result in an expression:

Where $\beta = \lambda \mu / 4\pi$, with μ the linear absorption coefficient (I = I_oe^{- μ t}).

See Appendices 1 & 2 for more details

The index of refraction for x-rays was first calculated by Charles Darwin in 1914. More about Darwin a little bit later.



SNELL'S (OR THE SNELL-DECARTES) LAW



The reflection and refraction of x-rays can be treated as any other electromagnetic wave traveling in a medium with index of refraction n_1 encountering a boundary with another material with index of refraction n_2 .

Willebrord Snellius

The resultant kinematic properties (which follow from the wave nature of the radiation at boundaries) are:

- The angle of incidence equals the angle of reflection
- n₁ sin(φ₁) = n₂ sin(φ₂) (Snell's Law), where the φ's are measured with respect to the boundary normal



Typical values for n_2 (at 5890Å) are: water: $n_2 = 1.33$ glass: $n_2 = 1.52$



For x-rays, the direction of propagation bends away from surface normal.



CRITICAL ANGLE FOR TOTAL EXTERNAL REFLECTION

Let an x-ray (in vacuum, where $n_1 = 1$) impinge on a material with index of refraction n_2 . From Snell's Law (when $\phi_2 = 90^\circ$), we have:

 $n_1 sin(\phi_c) = n_2 sin(90)$

 $\cos(\theta_{c}) = n_{2}\cos(0) \quad (\theta = 90 - \phi)$

 $\cos(\theta_c) = n_2$

Expanding the cosine of a small angle and substituting for n_2 gives:

1 -
$$(\theta_c)^2/2 = 1 - \delta$$

 $\theta_c = (2\delta)^{1/2}$

 θ_c is the so-called **critical angle**, the angle at which there is total external reflection and the material behaves like a mirror.

Recall that the typical values for δ at 1 Å is 10⁻⁵ to 10⁻⁶ and so the critical angle is going to be about 10⁻³ or a few milliradians





X-RAY REFLECTIVITY

The amplitude of the reflected wave can be determined through the Fresnel equations. Sparing you the details, the intensity ratio of the reflected and incident beam is given by:



From the Fresnel equations it can be shown that:

 Below θ_c, there is unit reflectivity (when β, the absorption equals 0)



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ENERGY CUTOFF FOR A FIXED ANGLE OF INCIDENCE MIRROR

Often mirrors are used as first optical components. This means a **polychromatic incident beam strikes the mirror at some fixed angle.**

The relationship for the critical angle and wavelength can be re-written in terms of a critical energy, E_c , for a fixed angle of incidence θ . Since $E = hc/\lambda$, I can re-write this for a fixed θ , and determine the maximum energy, E_c , that will be totally reflected by the mirror.

Reflectivity as a function of θ , R(θ)

Critical angle, $\theta_{\boldsymbol{c}}$, for fixed wavelength λ

 $\theta_{c} = (2\delta)^{1/2} = \lambda (n_{e}r_{e}/\pi)^{1/2}$

Reflectivity as a
function of energyCritical energy, E_c for fixed angle θ R(E) $E_c = hc/\lambda_c = (hc / \theta) (n_e r_e / \pi)^{1/2}$



For a fixed angle of incidence, you can vary the critical (cut-off) energy by coating the mirror with materials of different electron densities, n_e .

X-RAY MIRRORS

- Because the incidence angle are small (a few milliradians) to capture the full extent of the beam (say 1 mm or so), xray mirrors tend to be very long (sometimes over a meter).
- Low-pass filters
 - mirrors can be used to effectively suppress high energies
 - mirrors are designed so that the cutoff energy, E_c, can be varied by having several different coatings deposited on the mirror substrate
- Mirrors can effectively remove a considerable amount of the heat in the raw (incident) beam and reduce the thermal loading on downstream optics.



Courtesy Chandra mission website http://chandra.harvard.edu



Chandra's mirrors are positioned so they're almost parallel to the entering X-rays. The mirrors look like open cylinders, or barrels. The X-rays skip across the mirrors much like stones skip across the surface of a pond.

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Water cooled mirror in its vacuum tank.



MIRRORS AS FOCUSING OPTICS

One-dimensional focusing, collimating, etc.

- An ellipse is the ideal shape for a reflecting surface for point-to-point focusing. (A source at one foci will be imaged at the other foci.)
- Collimation can be achieved by a parabola if the source is placed at the focal point. (This is simply an ellipse with the second focal point at infinity.)
- In many cases cylindrically shaped mirrors are used rather than ellipses and parabolas since they are considerably easier to fabricate. However, can this introduces aberations into the system if the difference between the ideal shape and cylinder is large.

Focal length, $f = [R_m \sin \theta]/2$. When we plug this into the so-called lens formula: $\frac{1}{f} = \frac{1}{F_1} + \frac{1}{F_2}$ and solve for the radius of curvature, we get $R_m = [2/\sin \theta] [F_1 F_2/(F_1 + F_2)]$. Typically θ is a few milliradians, $\sin \theta \approx \theta$ and so if

 $F_1 = F_2 = 30$ m, then the radius of curvature, R_m , is around 10 kilometers.



focus

R

source

FOCUSING IN TWO DIMENSIONS WITH MIRRORS

Two-dimensional focusing (toroids and ellipsoids)

- An ellipsoid is the ideal shape for a reflecting surface for point-to-point focusing.
- Bent cylinders are often used in place of an ellipsoid. The sagittal radius, R_s , is given by:



 $R_s = R_m \sin^2 \theta$

In our example, from the last slide, θ = 3 mrad and R_m = 10 km so the sagittal radius would be:

 $R_s = 9 \text{ cm}$



FOCUSING IN TWO DIMENSIONS - KB SYSTEMS

Another system that focuses in two dimensions consists of a set of two orthogonal singly focusing mirrors, off which incident X-rays reflect successively, as first proposed in 1948 by Kirkpatrick and Baez (KB).

This system allows for easier fabrication of the mirrors and is used frequently at synchrotron sources.



SLAC, Stanford University







HIGH-BRIGHTNESS SOURCES PUT STRINGENT DEMANDS ON MIRROR QUALITY

The mirrors requirements are very stringent if you want to use them for focusing or to preserve the x-ray beam brightness.



Sources of errors in mirrors

- (a) long range slope errors
- (b) medium range slope errors
- (c) surface roughness
- (d) sum of all three errors

If we hope to focus the x-ray beam to 20 nm, the specifications required are:

- slope error must be < 0.03 microradians (rms)
- surface roughness < 1 nm (rms)

over the length of the mirror.





DIFFRACTIVE OPTICS

By far, the most commonly used optical component for x-rays are crystals satisfying Bragg's law, i.e.,



- In nearly all cases, perfect single crystals are used as the diffractive elements since:
 - they have a reflectivity near unity (more later) _
 - the physics is well understood and components can be fabricated with predicted characteristics
 - If designed properly, they preserve the beam brightness





William Henry Bragg William Lawrence Bragg

The Braggs shared the 1915 Nobel Prize in Physics.

Images from:

http://www4.nau.edu/microanalysis/Microprobe-SEM/History.html



*"The Diffraction of Short Electromagnetic Waves", W.L. Bragg, Proc. Cam. Phil. Soc. 17, p43 (1913) Read November 11, 1912



DIFFRACTION FROM PERFECT CRYSTALS

The theory that describes diffraction from perfect crystals is called <u>dynamical diffraction theory</u> (as compared with kinematical theory, which describes diffraction from imperfect or mosaic crystals) first proposed in 1914 by Charles Darwin in two seminal papers.



Mosaic crystal model



Perfect crystal model

The name "dynamical diffraction" was coined due to the fact that, during the diffraction process from perfect single crystals, there is a dynamic interplay between the incident and scattered beam, which can be comparable in strength.

In the case of a strong reflection from a perfect crystal of a monochromatic x-ray beam, the penetration of the x-rays in to the crystal is not limited by the (photoelectric) absorption, but the beam is attenuated due to the reflecting power of the atomic planes. (This type of attenuation is called "extinction".)



http://www.eoht.info/p age/C.G.+Darwin

" if the crystal is perfect all the radiation that can be reflected is so, long before the depth at which the rays at a different angle are appreciably absorbed."



TWO IMPORTANT CONSEQUENCES OF LIMITED PENETRATION IN DIFFRACTION FROM PERFECT CRYSTALS

The limited penetration due to extinction (reflection by the atomic planes) means:

- At the Bragg condition, the x-ray beam is limited in the amount of materials it "sees"
- and hence the scattered beam can get in and out of the crystal with little loss of amplitude from (photoelectric) absorption.

Consequence #1:

There is a finite angular width over which the diffraction occurs. This is often called the <u>Darwin width</u>, ω_D, and depends on the strength of the reflection (hkl) and wavelength.

Consequence #2:

The reflectivity over this narrow Darwin width is nearly unity, even in crystals with a finite absorption.



REAL WORLD PERFECT CRYSTALS

Perfect single crystal optics are used as the diffractive elements since:

- they have a reflectivity near unity
- the physics is well understood and components can be fabricated with predicted characteristics
- If designed properly, they preserve the beam brightness

At first glance, requiring the use of only perfect crystals for x-ray optical components may seem very limiting. However, <u>silicon</u> <u>and germanium</u>, are readily available (due to their use in the semiconductor industry) and are grown in large boules that are relatively inexpensive.



 Image: Simple state stress
 Simple state stress

 Simple state state stress
 Simple state stress

 Simple state state



components.

PERFECT CRYSTAL MONOCHROMATORS

The most frequent use of perfect crystal optics are for x-ray monochromators. They simply use Bragg's Law to select a particular wavelength (or energy, since $\lambda = hc/E$):

$$\lambda = 2d \sin(\theta).$$

If we differentiate Bragg's Law, we can determine the energy resolution of the monochromator.



A value of ω_D for the (111) reflection in silicon at 8 keV (1.5Å) is about 8 sec of arc or 40 microradians. Recall that, for an undulator, the opening angle is about 10 microradians at the APS. Here the energy resolution of the mono is determined by the crystal.



REAL MONOCHROMATORS

The most common arrangement is the double-crystal monochromator. It:

- is non-dispersive, that is all rays that diffract from the first crystal simultaneously diffract from the second crystal (if same crystals with same hkl's are used)
- keeps the beam fixed in space as the energy is changed.

There is little loss in the throughput because the reflectivity is near unity over the Darwin width.

Monochromators need to be cooled to maintain the desired properties.

 Silicon monochromators are often liquid N₂ cooled to enhance thermal properties (higher conductivity and coefficient of thermal expansion goes through a zero at about 120° K.

See Appendix 3 for more information regarding thermal issues for monochromators.



LN COOLED SILICON MONOCHROMATORS



HIGH-ENERGY RESOLUTION OPTICS

- For techniques such as inelastic x-ray scattering, additional spectral filtering for higher-energy resolution (ΔE/E ~ 10⁻⁵ – 10⁻⁶) is required for both the x-rays impinging on the sample as well as for those that scatter from it.
- To achieve energy resolution at this level requires special geometries for the optical components, often Bragg scattering with the angle of incidence near 90°.
- Recall that: $\Delta \lambda / \lambda = \Delta E/E = \cot(\theta) \Delta \theta$, so this can be made small by $\theta \rightarrow 90^{\circ}$



DIFFRACTIVE FOCUSING OPTICS: X-RAY ZONE PLATES

Zone plates are diffraction gratings, that is, structures composed of alternating concentric zones of two materials with different (complex) refractive indices.

The focusing capability is based on constructive interference of the wavefront modified by passage through the zone plate.

The wave that emerges from the zone plate is the superposition of spherical waves, one from each of the zones.

The wavefront modification is obtained through the introduction of a relative change in amplitude or phase in the beams emerging from two neighboring zones.

JOURNAL OF THE OPTICAL SOCIETY OF AMERICA

VOLUME 51, NUMBER 4

APRIL, 1961

Fresnel Zone Plate for Optical Image Formation Using Extreme Ultraviolet and Soft X Radiation

> ALBERT V. BAEZ Smithsonian Astrophysical Observatory, Cambridge, Massachusetts (Received April 25, 1960)



http://www.psi.ch/lmn/electron-beamlithography









Cape Meares Lighthouse (Oregon); first-order Fresnel lens

The radius of the nth zone is therefore:

$$r_n = (R_n^2 - f^2)^{1/2} = [(f + n(\lambda/2))^2 - f^2]^{1/2}$$
$$= [nf \lambda + n^2(\lambda^2/4)]^{1/2}$$

If $f \gg n\lambda$, as is usually the case with hard x-rays, then:

$$r_n = (nf\lambda)^{1/2}$$

These are chromatic, i.e. the focal length is dependent on x-ray wavelength.

Zone plate



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In general, the size of the focal spot from the zone plate is determined by the width of the outermost ring, Δr_{out} , and is given by:

$$\Delta x = 1.22 \Delta r_{out}$$
.



HARD X-RAY PHASE ZONE PLATES

The difficulty with making zone plates at hard x-ray energies is one of fabrication. You need:

- small width outermost zone for focusing (less than 50 nms) but it has to be thick (high) to totally absorb the unwanted waves
- i.e. the aspect ratio (height/width) is very large 10² and therefore difficult (i.e. impossible) to fabricate

An alternative to "blocking" out those rays that are out of phase (as in an **amplitude zone plate**), the thickness of the material can be adjusted so that the wave experiences a phase shift of π .

Phase zone plates have a much better efficiency than amplitude zone plates (10% efficiency for amplitude zone plates vs 40% for phase zone plates).

Multiple zone plates can be "stacked" to increase the effective thickness, but alignment is critical.

See Appendix 5 for an interesting alternative method for zone plates fabrication.



Stacking for high efficiency



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REFRACTIVE FOCUSING OPTICS: X-RAY LENSES

Roentgen's first experiments convinced him that x-rays could not be concentrated by lenses; many years later his successors understood why (i.e., index of refraction is very close to 1).

Refractive lenses were considered by Kirkpatrick and Baez in 1948 for focusing but were abandoned for crossed mirrors.



Unfortunately materials of large δ are also strong absorbers, because the absorption coefficient increases much more rapidly than δ with increasing atomic number. Therefore, an element of low atomic number, such as beryllium, is typically used.

- For a single concave lens: $1/F = \delta(1/R)$
- Plugging in some numbers, suppose that:

R = 1 mm δ≈ 10⁻⁵

• Then the focal length, F, would be at 100 m!



COMPOUND REFRACTIVE LENSES



FOCUSING IN WITH REFRACTIVE LENSES

2-D lenses typically "embossed" and typically made from Be, Al or Nickel Spherical lenses are easy to make but suffer from spherical aberrations. Paraboloids eliminate spherical aberrations.



en&frames=&content=crl#Focusingmethods



Planar technologies for 1-D focusing

- Leverage planar technologies from micro-electronics industry
- Fabricate compound lens systems in a small space
- Small radius means moderate focal spots with a single lens or nano-focusing with a moderate number of lenses



core

CURRENT OPTICS R&D ACTIVITIES

X-ray optics is still an active area of research at both universities and national laboratories (in particular here at the APS).

- Adaptive mirrors
- Nanodiffractive optics
- Simulation tools.



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Synchrotron

Radiation

SCIENTIFIC

REPORTS

Received 13 November 2013

Accepted 28 November 2013

Published 20 December 2013

11 nm hard X-ray focus from a

A hybrid method for X-ray optics simulation:

combining geometric ray-tracing and wavefront

large-aperture multilayer Laue lens

Xiaojing Huang¹, Hanfei Yan¹, Evgeny Nazaretsk¹, Raymond Conley^{1,2}, Nathalie Bouet¹, Juan Zhou¹, Kenneth Lauer¹, Li Li¹, Daejin Eom¹*, Daniel Legnini², Ross Harde², Ian K. Robinson^{3,4} & Yong S. Chu¹

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Soft X-ray Optics

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APPENDICES



APPENDIX 1A: DIELECTRIC CONSTANT AND THE DRUDE MODEL

The dielectric constant, κ , is defined as follows:

 $\kappa = D/E = (E + 4\pi P)/E = 1 + 4\pi (P/E)$

For a single electron:	P = -ex	
and for multiple electrons:	P = -exn _e	(n _e is the number of electrons/unit volume)

In the Drude model, the frequency of the collective oscillations of the electron gas around the positive ion background is the so-called plasma frequency and equal to:

$$ω_o = [4π n_e e^2/m]^{1/2}$$
.

If we assume a simple harmonic approximation then:

 $F=ma=mx^{"}=-eE-kx$

where k is the "spring constant" associated with ω_0 (= [k/m]^{1/2}).



APPENDIX 1B: X-RAY INDEX OF REFRACTION

If x (from the previous page) has a solution of the form $x = Ae^{i\omega t}$, solving for x we get:

$$x = (e/m)E/(\omega_0^2 - \omega^2)$$
 and $P = -(e^2/m)n_eE/(\omega_0^2 - \omega^2)$

Using this simple model, one can then calculate the polarizability of the material:

$$\kappa = 1 + 4\pi (P/E) = 1 + 4\pi (e^2/m)n_e [1/(\omega_o^2 - \omega^2)]$$

For Si, $n_e = 7 \times 10^{23} \text{ e/cm}^3$ and so the plasma frequency is:

 $\omega_0 = 5 \times 10^{16} / \text{sec}$

For a 1 Å x-ray, the angular frequency, $\omega (= [2\pi c/\lambda])$, is **2 x 10¹⁹/sec (>> \omega_o)** and so we can write:

$$\kappa = 1 + 4\pi (e^{2}/m)n_{e} [1/(\omega_{o}^{2} - \omega^{2})] \approx 1 - 4\pi (e^{2}/m)n_{e} [1/(\omega^{2})]$$

 $n = \kappa^{1/2} = [1 - (n_e(e^2/mc^2)\lambda^2/\pi)]^{1/2} \approx 1 - (n_e r_e/2\pi)\lambda^2$



APPENDIX 2A: INCLUSIONS OF ABSORPTION IN THE (COMPLEX) INDEX OF REFRACTION

This simple model did not include any absorption of the incident radiation. A more detailed calculation would result in an expression:

$$n = 1 - \delta - i\beta$$

where $\delta = (n_e r_e/2\pi)\lambda^2$ and $\beta = \lambda \mu/4\pi$, with μ the linear absorption coefficient (I = I_oe^{- μ t}).

APPENDIX 2B: INDEX OF REFRACTION FOR X-RAYS IS <1

OK, isn't $V_{group} = (c/n)$? If n < 1, doesn't that mean the x-rays are traveling faster than the speed of light? **NO!**

$$V_{\text{group}} = \frac{d\omega}{dk} \quad \text{and} \quad \omega = \frac{ck}{n} \quad \text{so} \quad V_{\text{group}} = \frac{d}{dk} \left(\frac{ck}{n} \right); \quad k = \frac{2\pi}{\lambda} \quad n = 1 - \frac{2\pi n_e r_e}{k^2}$$
$$V_{\text{group}} = \frac{d}{dk} \left[\frac{ck}{1 - \frac{2\pi n_e r_e}{k^2}} \right] \approx \frac{d}{dk} \left[ck \left(1 + \frac{2\pi n_e r_e}{k^2} \right) \right] = c \frac{d}{dk} \left[\left(k + \frac{2\pi n_e r_e}{k} \right) \right] = c \left(1 - \frac{2\pi n_e r_e}{k^2} \right)$$



APPENDIX 3A: THERMAL LOADING ON OPTICS

Along with the enormous increase in x-ray beam brilliance from insertion devices comes unprecedented powers and power densities that must be effectively handled so that thermal distortions in optical components are minimized and the full beam brilliance can be delivered to the sample.

Process	<u>Approx. Heat Flux (W/r</u>	<u>nm²)</u>
Fission reactor cores	1 to 2	
Interior of rocket nozzle	10	
Commercial plasma jet	20	
Sun's surface	60	In order to maintain the beam intensity and
Fusion reactor components	0.05 to 80	collimation (i.e., brilliance) through the
Meteor entry into atmosphere	100 to 500	issue of thermal management.
APS insertion devices (2.4 m and 100 mA)	10 to 160	

Total power from an undulator of length L and magnetic field B with I current in the storage ring is:

P[watts] = 0.633 E²[GeV] B²[T] I [mA] L [m]

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APPENDIX 3B: PROPERTIES OF SI, GE, AND C(DIAMOND)

Thermal gradients, ΔT , and coefficient of thermal expansion, α , contribute to crystal distortions:

 $\alpha \Delta T = \Delta d/d = \cot(\theta) \Delta \theta = \cot(\theta) \omega_{\rm D}.$

We therefore need to look for materials that have a very low coefficient of thermal expansion, α , and/or have a very high thermal conductivity, k, so that the material cannot support large ΔT 's.





APPENDIX 3C: FIGURE OF MERIT (FOM) FOR VARIOUS MATERIALS AND TEMPERATURES

These conditions motivate us to use cryogenically cooled silicon or room temperature diamond as high heat load monochromators.

FOM of various materials

	k - thermal	α - coef. of	k/α
material	conductivity	thermal expansion	FOM
Si (300°K)	1.2 W/cm-°C	2.3 x 10 ⁻⁶ /° K	0.5
Si (78°K)	14 W/cm-°C	-0.5 x 10 ⁻⁶ /° K	28
Dia. (300°K)	20 W/cm-°C	0.8 x 10 ⁻⁶ /° K	25



APPENDIX 4: HIGH ENERGY-RESOLUTION OPTICS

At $\theta = 89^{\circ}$, $\cot(\theta) = 1.7 \times 10^{-2}$. For E = 20 keV (0.64Å), then:

 $\Delta E = E \cot(\theta) \Delta \theta = (2 \times 10^4 \text{ keV})(1.7 \times 10^{-2})(10^{-5} \text{ rad}) = 3 \times 10^{-3} \text{ eV}.$

Note: For Si (111) at a Bragg angle of θ = 89°, the wavelength is 6.2Å (2 keV) and so to get near 20 keV at θ = 89°, we need to use a very high d-spacing such as Si (11 11 11).



A diced, high energy resolution inelastic x-ray spherical analyzer.



Inelastic scattering set-up at the 3-ID-C beam line at the APS. The sample is located in the right front corner of the photo. The analyzers are in the back and not visible.

The high energy resolution inelastic x-ray (HERIX) beamline at the APS with an array of analyzers.



APPENDIX 5: A NEW APPROACH TO FABRICATING ZONE PLATES – MULTILAYER LAUE LENSES (MLLS)

Start with a linear zone plate geometry and then use a Kirkpatrick-Baez configuration to get focusing in both directions



Each MLL comprises 1,588 layers (lines) The thinnest layer (line) is 5 nanometers thick

The MLL has a current focus of 11 nanometers at 12 keV and 16 nanometers @ 19 keV!

Using state-of-the-art deposition techniques, start with the thinnest layer first and fabricate a multilayer structure with the layer spacing following the Fresnel zone plate rule.

Slice and polish the multilayer structure to get a linear zone plate.

H. C. Kang, J. Maser, G. B. Stephenson, C. Liu, R. Conley, A. T. Macrander, and S. Vogt, "Nanometer Linear Focusing of Hard X Rays by a Multilayer Laue Lens," Phys. Rev. Lett. 96, 127401 (2006).



Wedged MLL



APPENDIX 5: MULTILAYER LAUE LENSES

- Technical approach
 - Crossed multilayer-based linear zone plate structure





